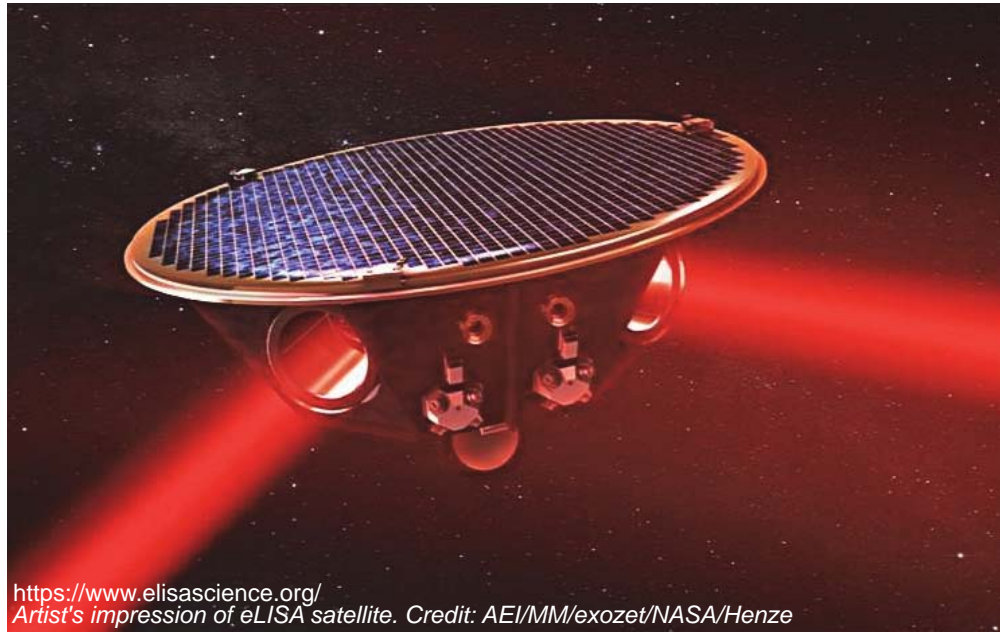


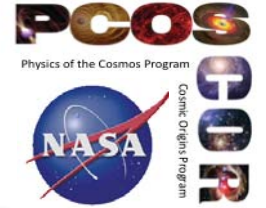
# Space-based Gravitational-wave Observatories (SGOs)



**Presented by Jeff Livas**  
**NASA Goddard Space Flight Center**  
**Greenbelt, MD 20771**

# Outline

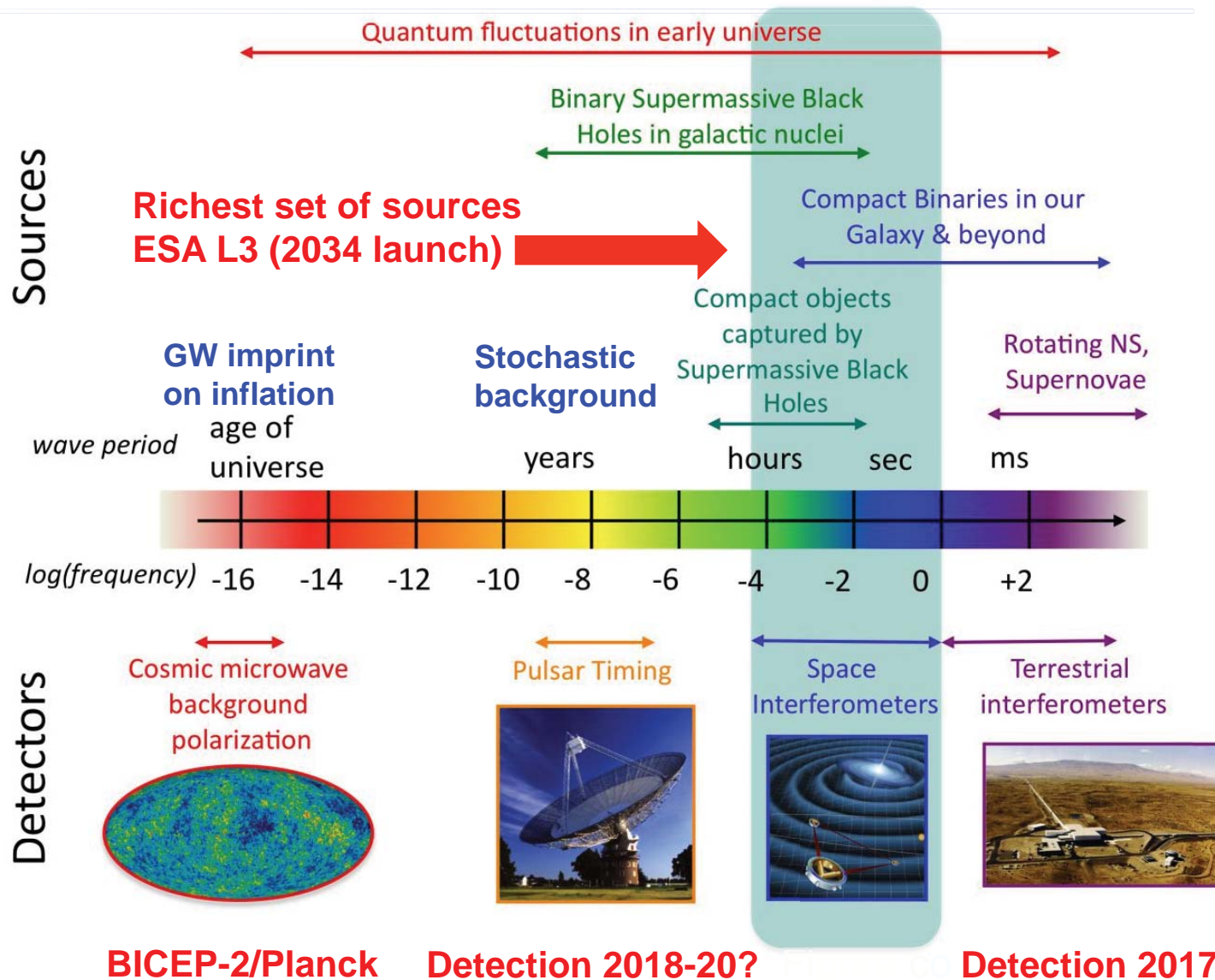
---



- **Why are SGOs important?**
- **Basic GW physics**
- **Science**
- **Mission description**
- **How it works – more detail**
- **Program status**
- **Summary**

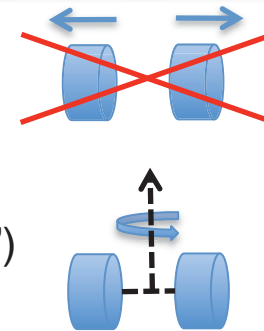
# Why is this important?

## The Gravitational Wave Spectrum



# Measurement Challenge

- **Lowest order radiator is a quadrupole**
  - Dipole radiation forbidden by conservation of momentum
  - Simplest quadrupole is a pair of masses rotating around their common center of mass (a “dumbbell”)
- **What is to be measured**
  - Time-varying strain ( $\Delta L/L$ ) in spacetime typically  $\sim 10^{-21} / \sqrt{\text{Hz}} = 10 \text{ pm}/10 \text{ Gm}/\sqrt{\text{Hz}}$
  - Variations are periodic or quasi-periodic between  $10^{-4}$  and  $1 \text{ Hz}$ , observable for months to centuries
- **Measurement concept**
  - Measure distance changes between free-falling mirrors
    - Test masses are the mirrors
    - Interferometric measurement of distance changes
  - Preferred measurement conditions
    - A long measurement path to make  $\Delta L$  large
    - A very quiet place to avoid disturbances to the test masses: **SPACE!**



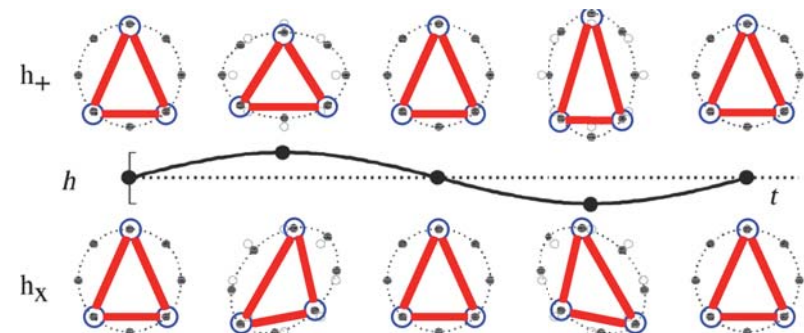
$h_+$  Polarization



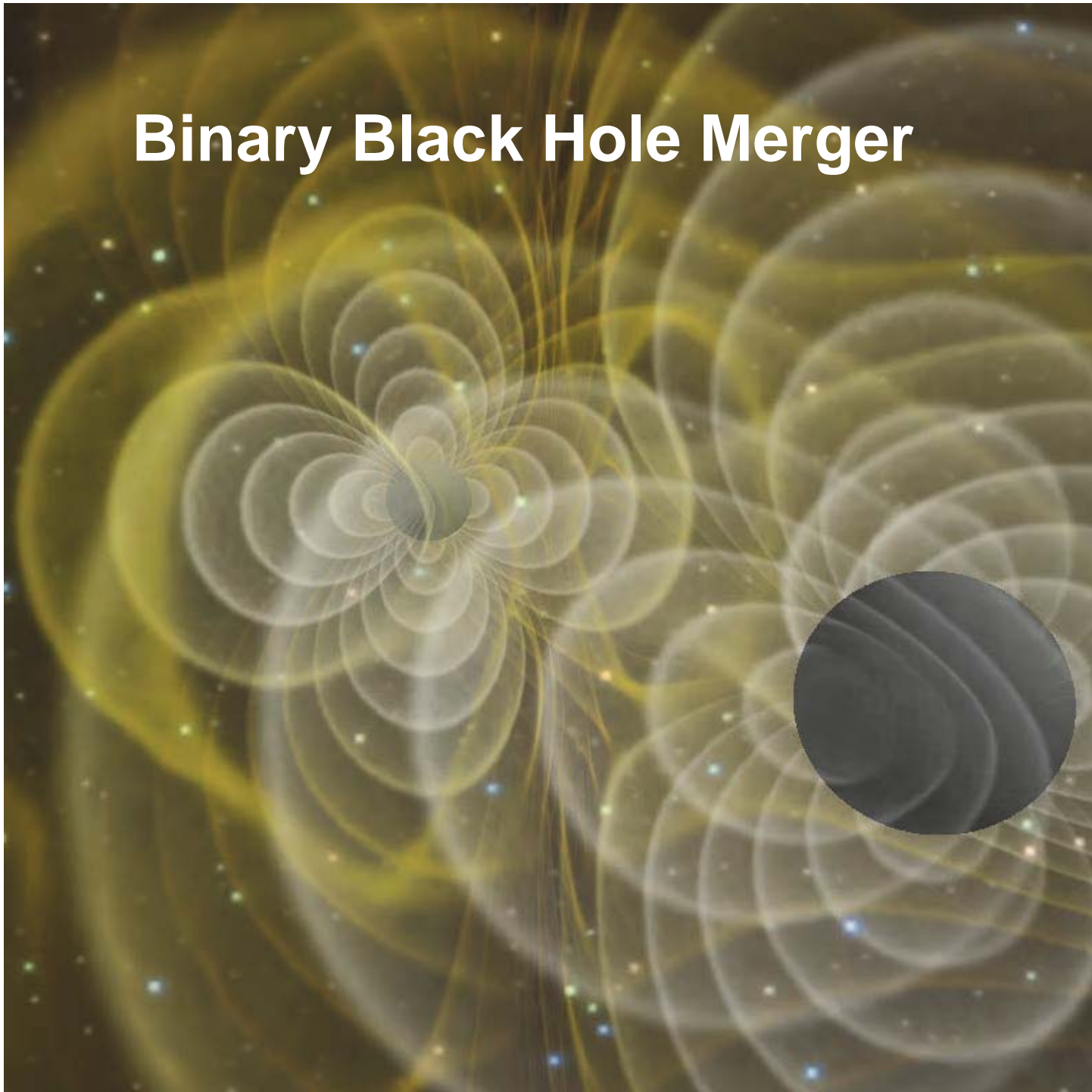
$h_x$  Polarization



Constellation Response

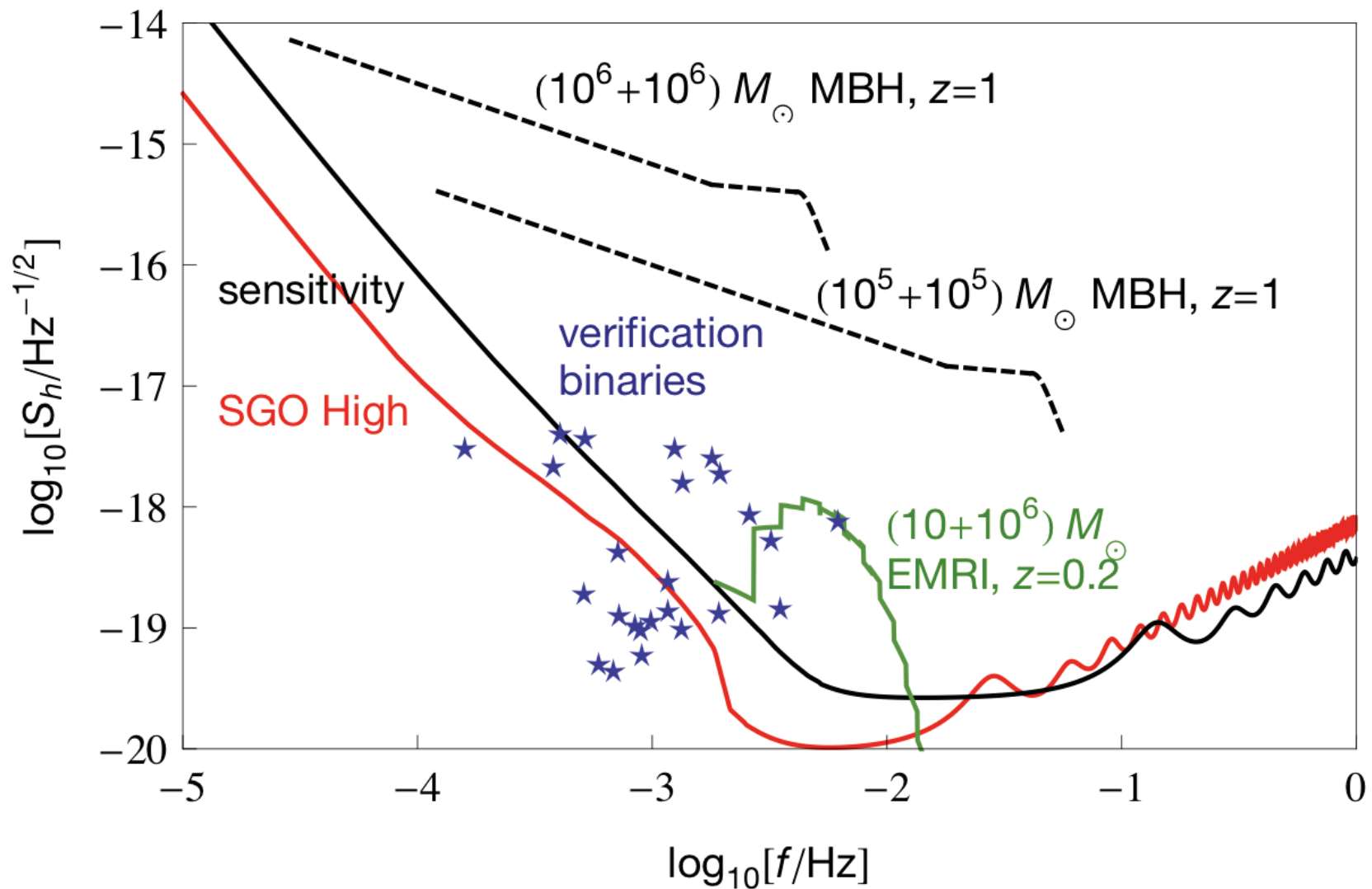


# Binary Black Hole Merger





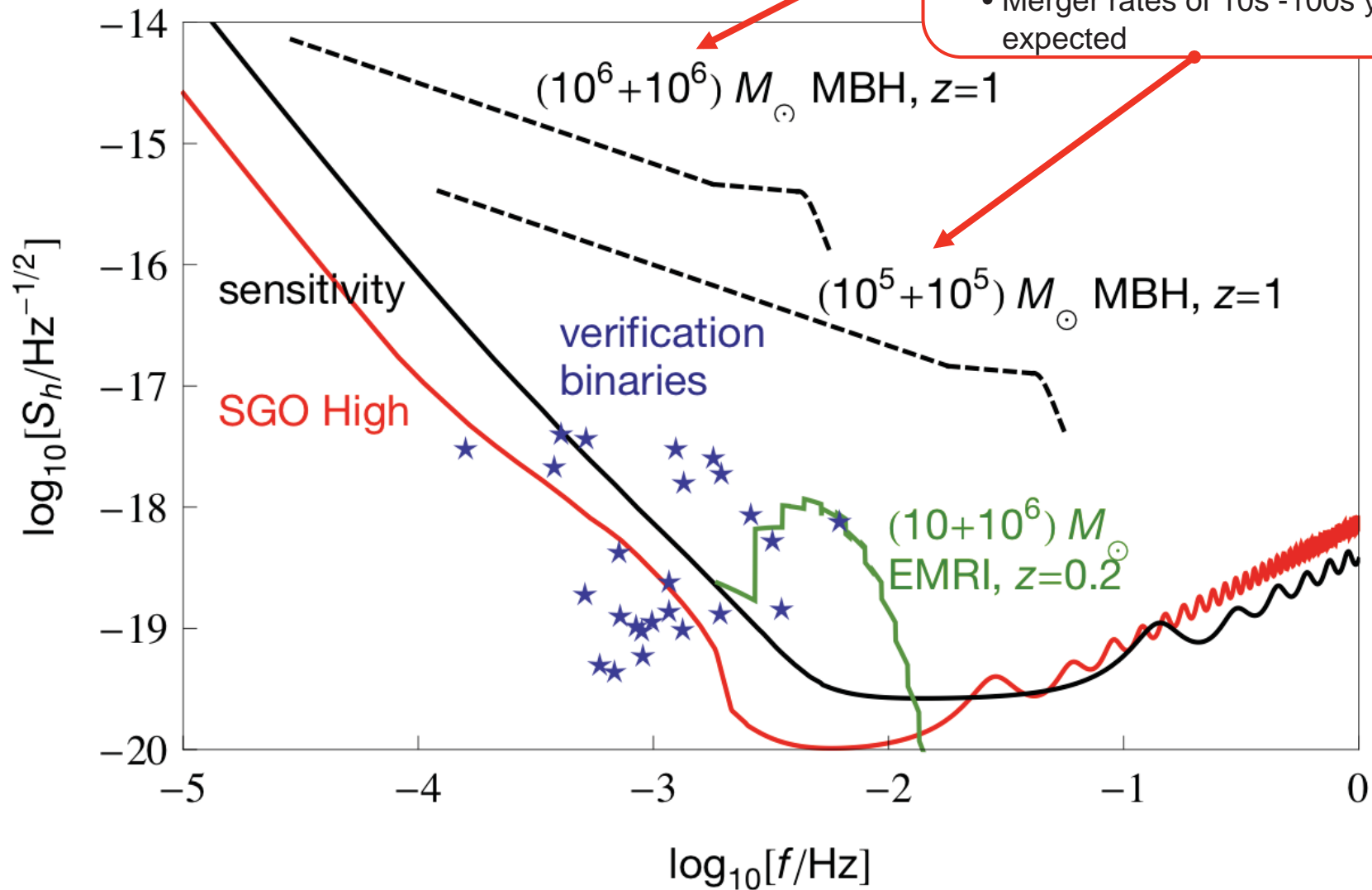
# Science Overview



# Science Overview

## Supermassive Black Hole Mergers

- Formation and growth of massive black holes: galaxy mergers
- Dynamical strong-field gravity
- Merger rates of 10s -100s  $\text{yr}^{-1}$  expected



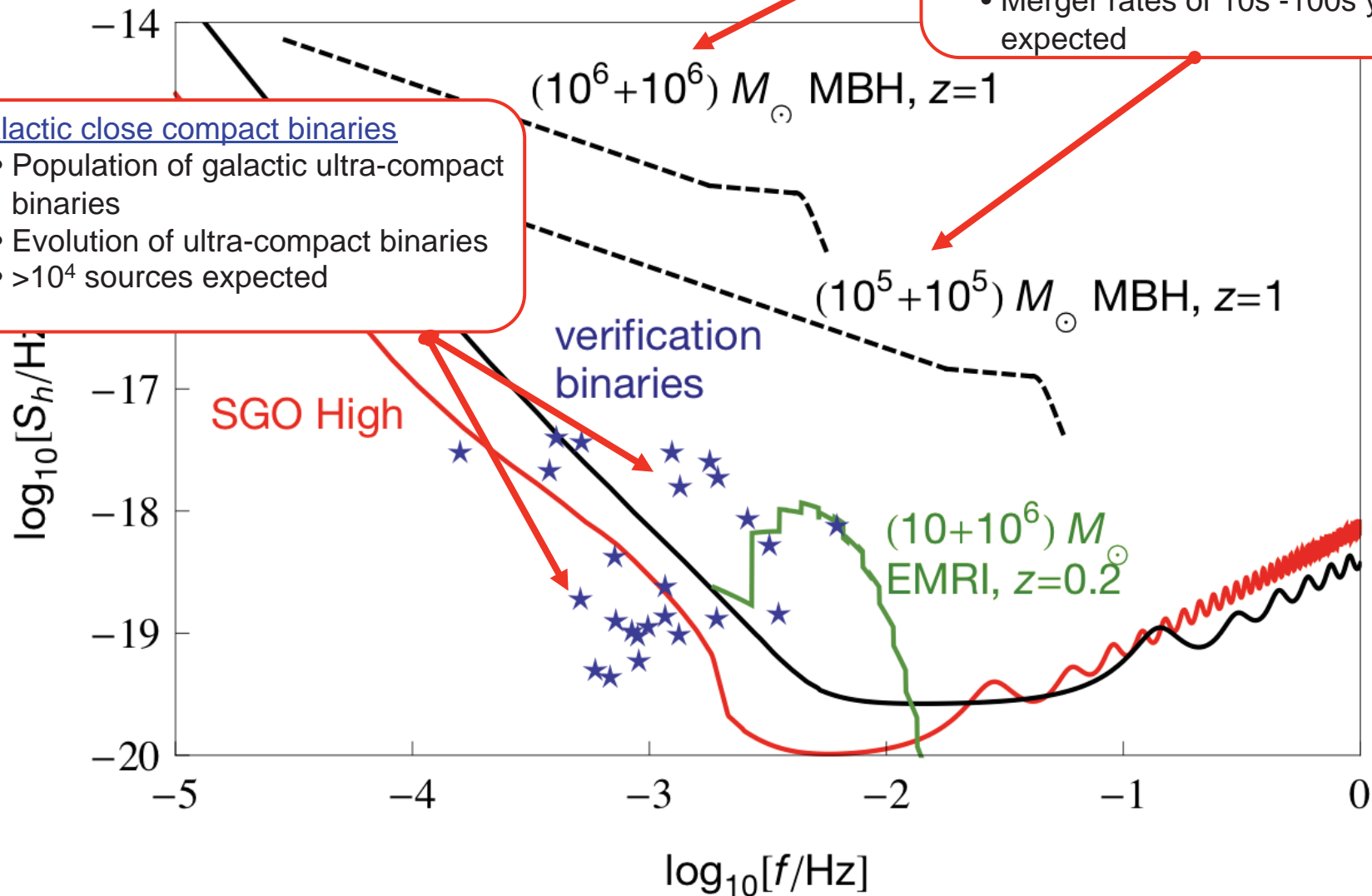
# Science Overview

## Supermassive Black Hole Mergers

- Formation and growth of massive black holes: galaxy mergers
- Dynamical strong-field gravity
- Merger rates of 10s -100s  $\text{yr}^{-1}$  expected

## Galactic close compact binaries

- Population of galactic ultra-compact binaries
- Evolution of ultra-compact binaries
- $>10^4$  sources expected





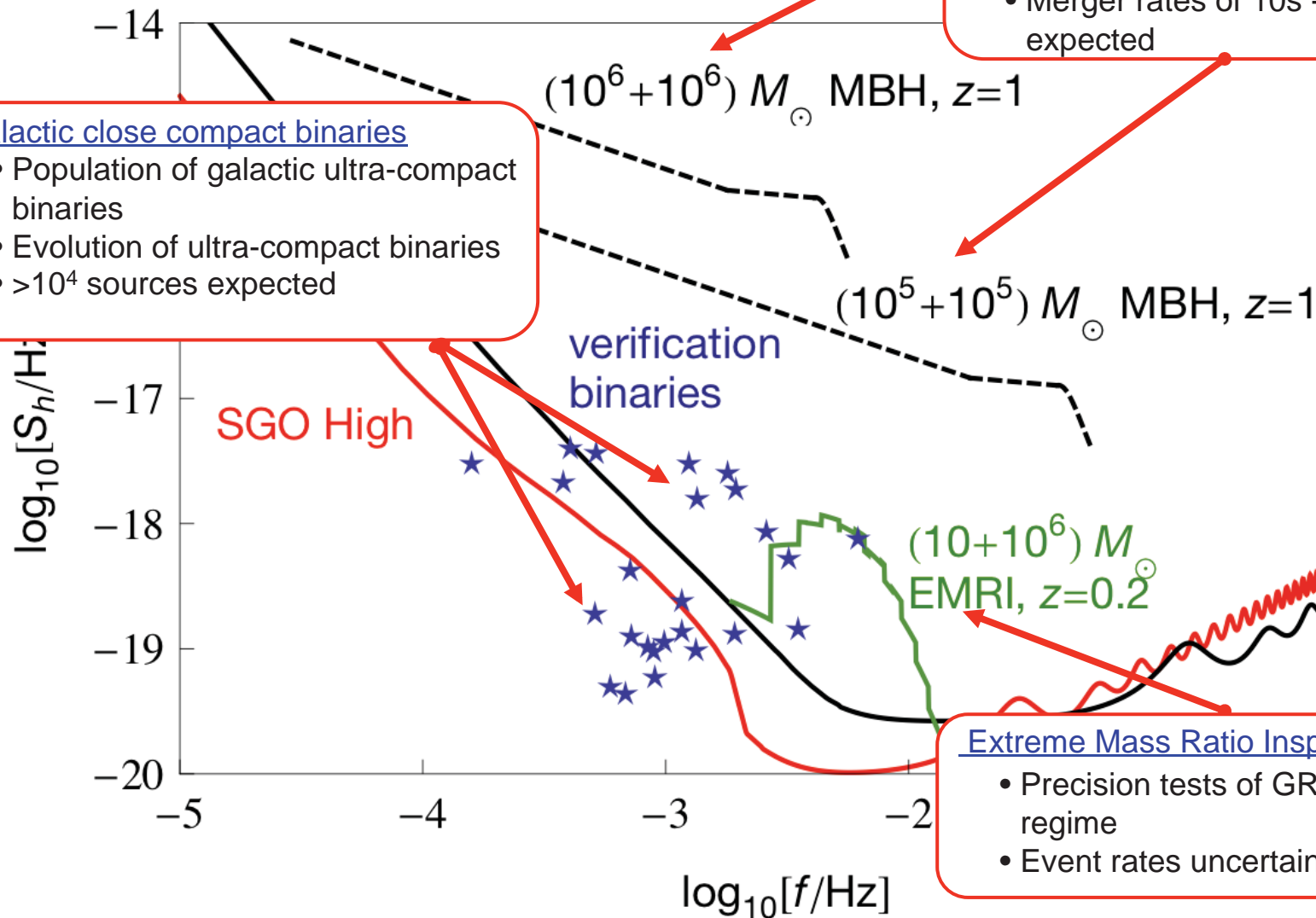
# Science Overview

## Galactic close compact binaries

- Population of galactic ultra-compact binaries
- Evolution of ultra-compact binaries
- $>10^4$  sources expected

## Supermassive Black Hole Mergers

- Formation and growth of massive black holes: galaxy mergers
- Dynamical strong-field gravity
- Merger rates of 10s -100s  $\text{yr}^{-1}$  expected



## Extreme Mass Ratio Inspirals (EMRIs)

- Precision tests of GR in strong-field regime
- Event rates uncertain

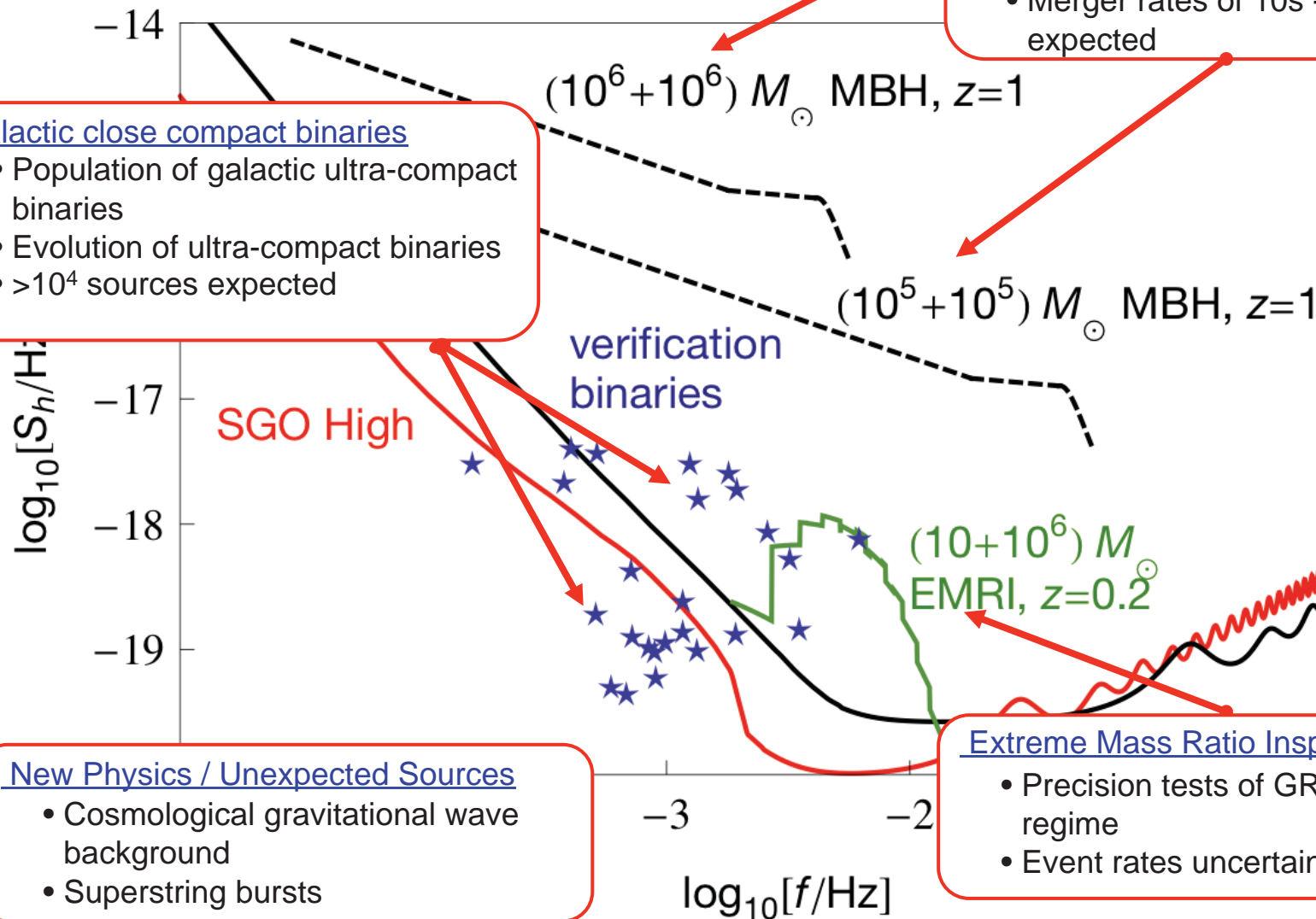
# Science Overview

## Supermassive Black Hole Mergers

- Formation and growth of massive black holes: galaxy mergers
- Dynamical strong-field gravity
- Merger rates of 10s -100s  $\text{yr}^{-1}$  expected

## Galactic close compact binaries

- Population of galactic ultra-compact binaries
- Evolution of ultra-compact binaries
- $>10^4$  sources expected



## New Physics / Unexpected Sources

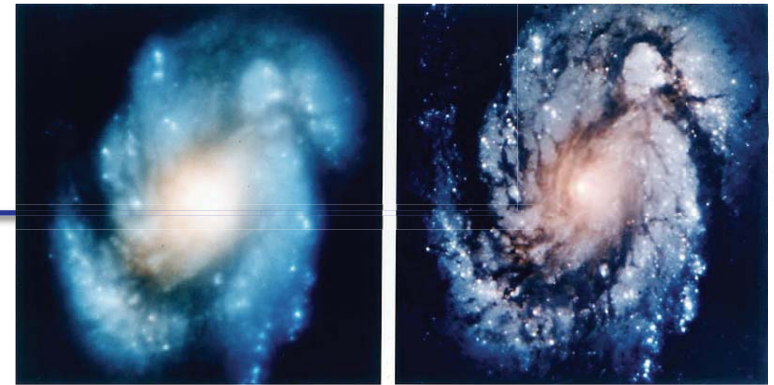
- Cosmological gravitational wave background
- Superstring bursts

## Extreme Mass Ratio Inspirals (EMRIs)

- Precision tests of GR in strong-field regime
- Event rates uncertain

# Not just detection...

- Detection already happened (direct + indirect...)
- Study growth of cosmic structure
- Test of GR in strong field limit
- Precise parameter estimation, including distances



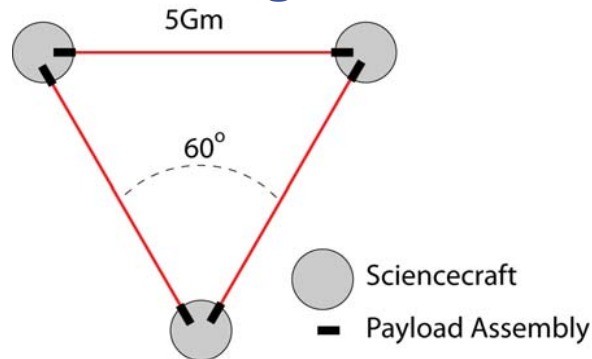
Quality vs Quantity

Number of Sources Observed	Classic LISA	SGO-Mid
Massive Black Hole Mergers	108-230	41-52
Detected @ $Z > 10$	3-57	1-4
Both mass errors $< 1\%$	67-171	18-42
One spine error $< 1\%$	49-130	11-27
Both spin errors $< 1\%$	1-17	$< 1$
Distance error $< 3\%$	81-108	12-22
Sky location $< 1 \text{ deg}^2$	71-112	14-21
Sky location $< 0.1 \text{ deg}^2$	22-51	4-8
Extreme-Mass-Ratio-Inspirals	800	35
Resolved Ultra Compact Binaries	40,000	7,000
Interacting UCB's	1,300	100
Detached UCB's	40,000	8,000
Sky location $< 1 \text{ deg}^2$	13,000	2,000
Sky loc $< 0.1 \text{ deg}^2$ + distance error $< 10\%$	8,000	800
Stochastic Bkgnd relative to LISA	1.00	0.20

Table courtesy Robin T. Stebbins  
With assistance from R. Lang, N. Cornish, and S. Larson

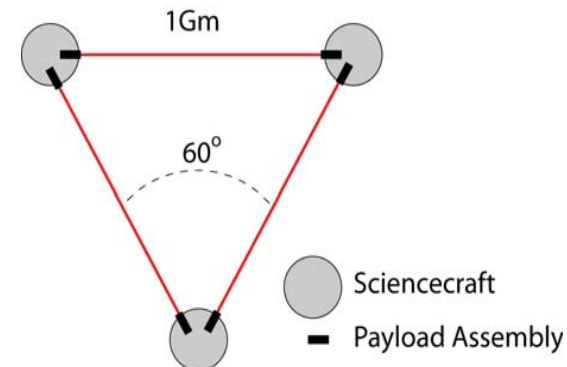
# SGO Mission Concepts

## SGO High



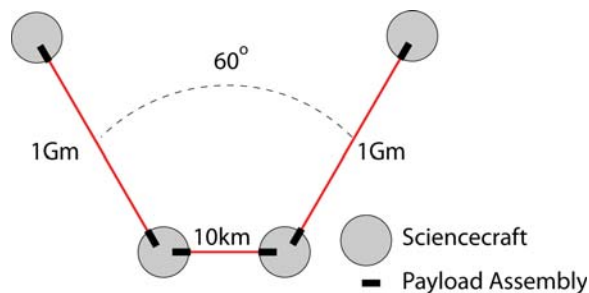
LISA concept with single-agency costing and all know cost reductions.

## SGO Mid



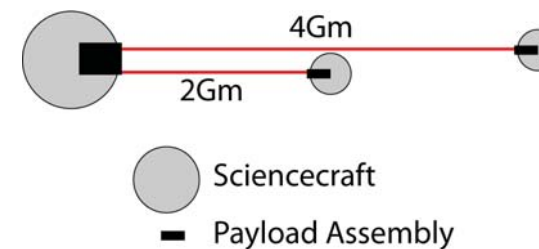
Minimum-cost three arm design with acceptable Decadal-survey science return.

## SGO Low



Two-arm version of SGO Mid

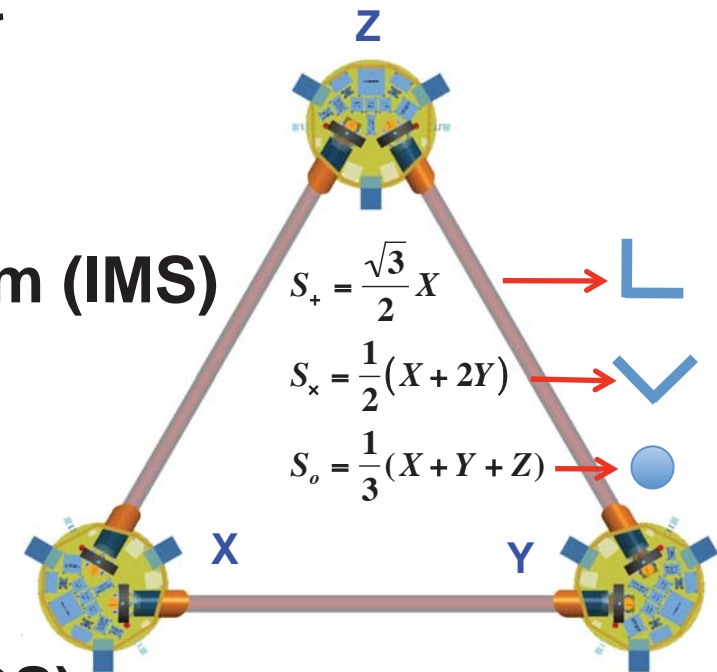
## SGO Lowest



Minimum two-arm mission

# How the science instrumentation works

- **The Constellation is the instrument**
  - Orbits passively maintain formation
  - “Sciencecraft” house test masses and interferometry
- **Interferometer Measurement System (IMS)**
  - Active transponder, phase-locked laser ranging system
  - Phasemeter records fringe signal
  - Laser frequency noise correction by pre-stabilization and post processing
- **Disturbance Reduction System (DRS)**
  - Free-falling test masses don’t contact the sciencecraft
  - Drag-free stationkeeping reduces sciencecraft test mass relative motion and force gradients
  - Design to limit thermal, magnetic, electrostatic, mechanical, self-gravity disturbances

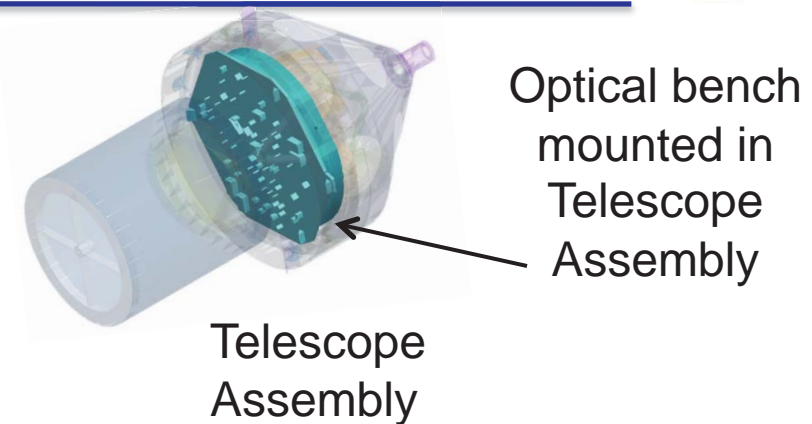




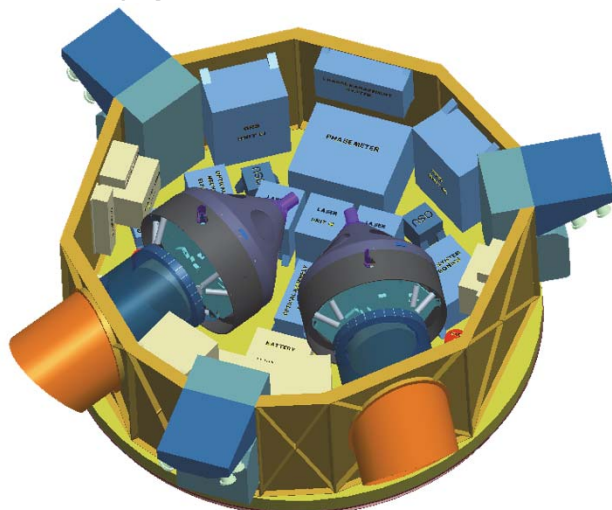
# Payload Integrated with Bus

## Payload systems

- Interferometer Measurement System (IMS)
  - Laser
  - Telescope
  - Optical bench
- Disturbance Reduction System (DRS)
  - Gravitational Reference Sensor (GRS)
  - $\mu\text{N}$  thrusters
  - Control laws

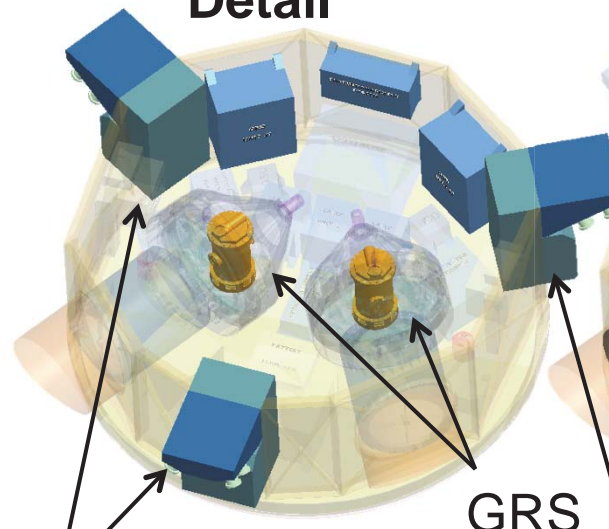


## Full Spacecraft Bus

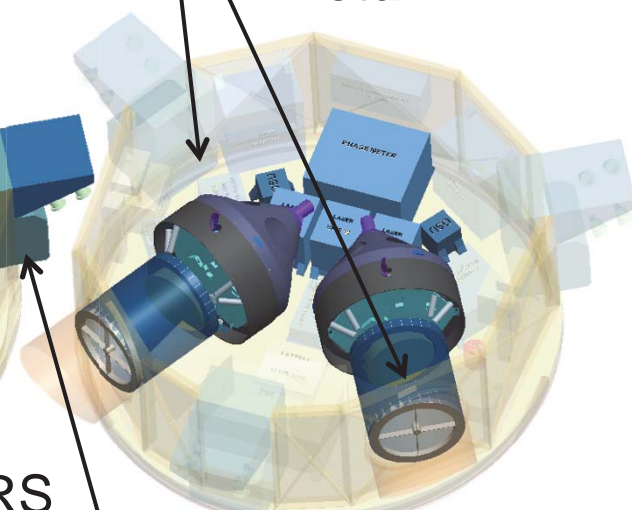


(Note: solar array not shown)

## DRS Detail

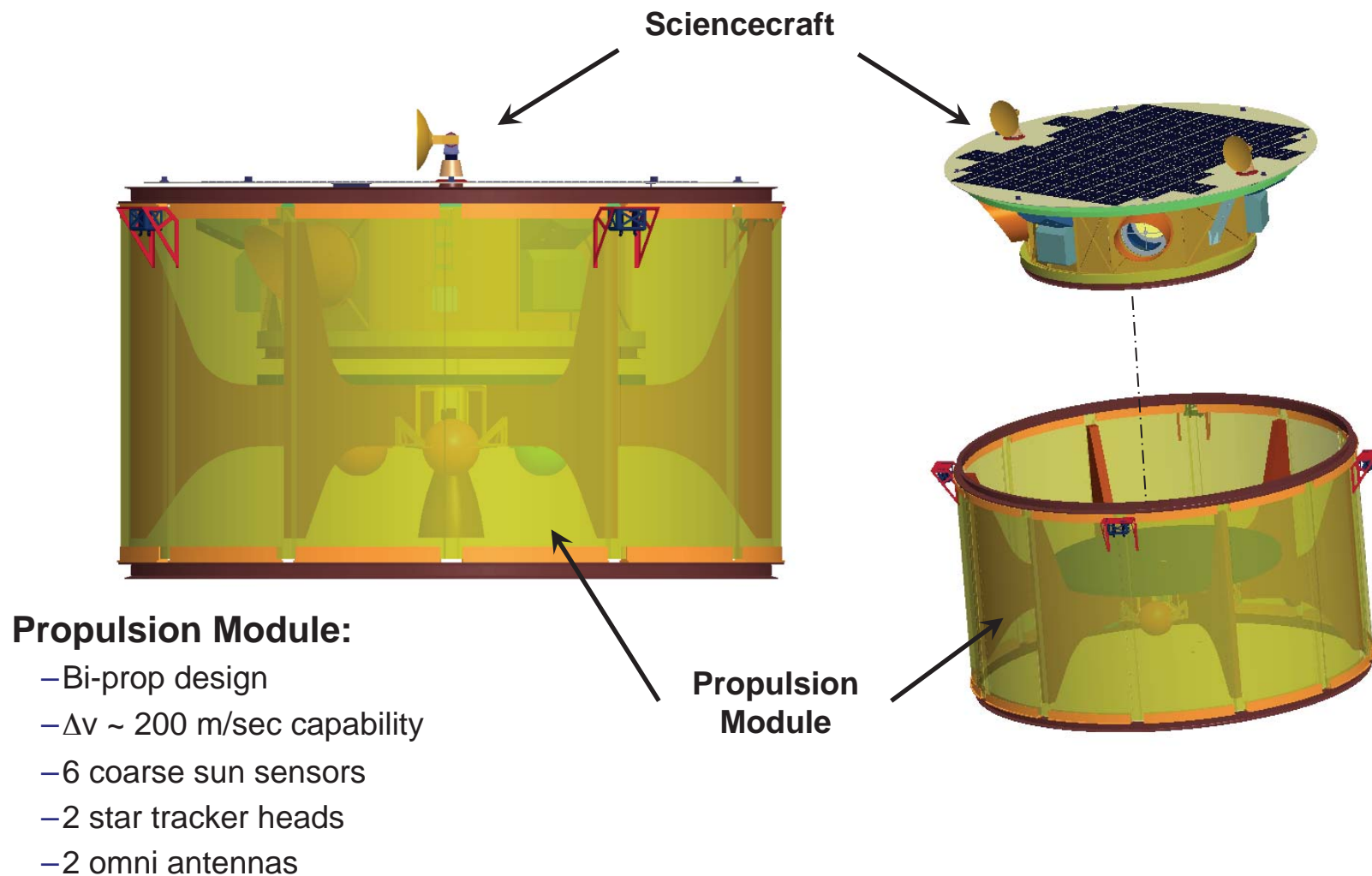


## IMS Detail





# Prop Module/Cruise Configuration

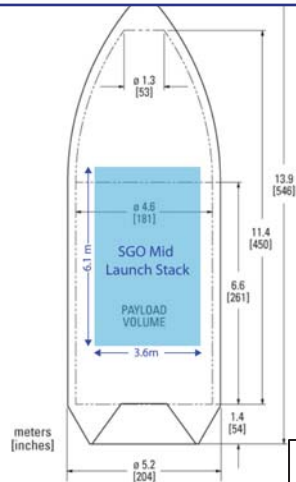


# Mission Timeline

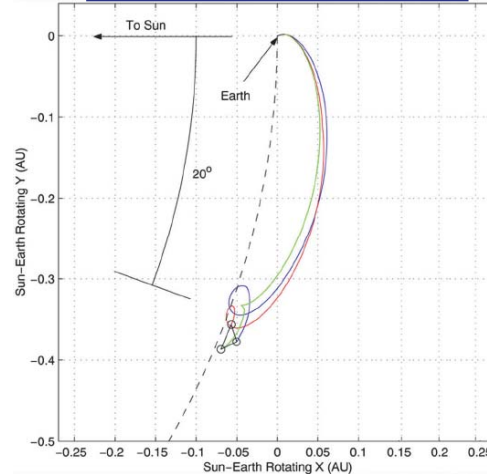
## Falcon Heavy EELV



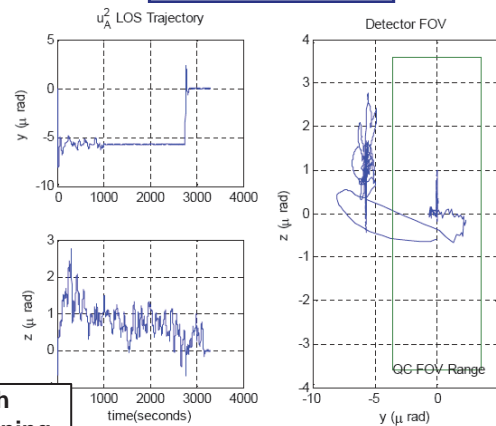
## Stack in Falcon 5 m PLF



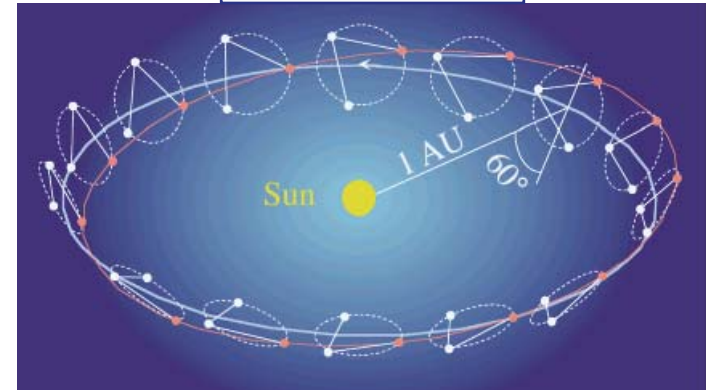
## Cruise Trajectories



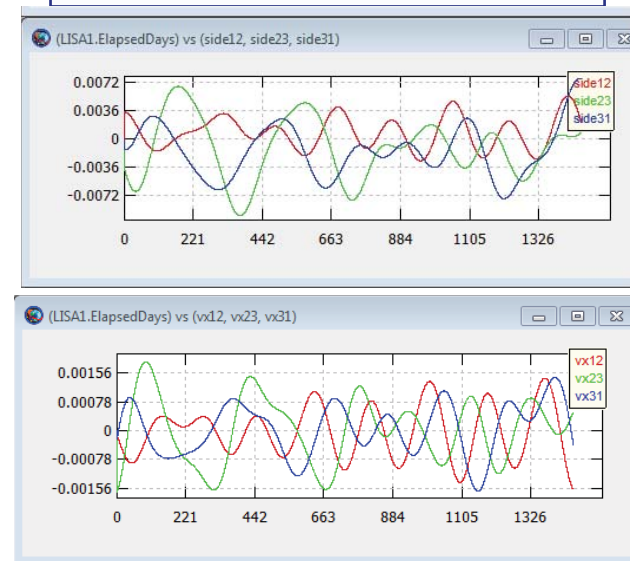
## Acquisition



## Science Orbits



## Doppler/Arm length changes



4 month  
commissioning

## Mission Timeline

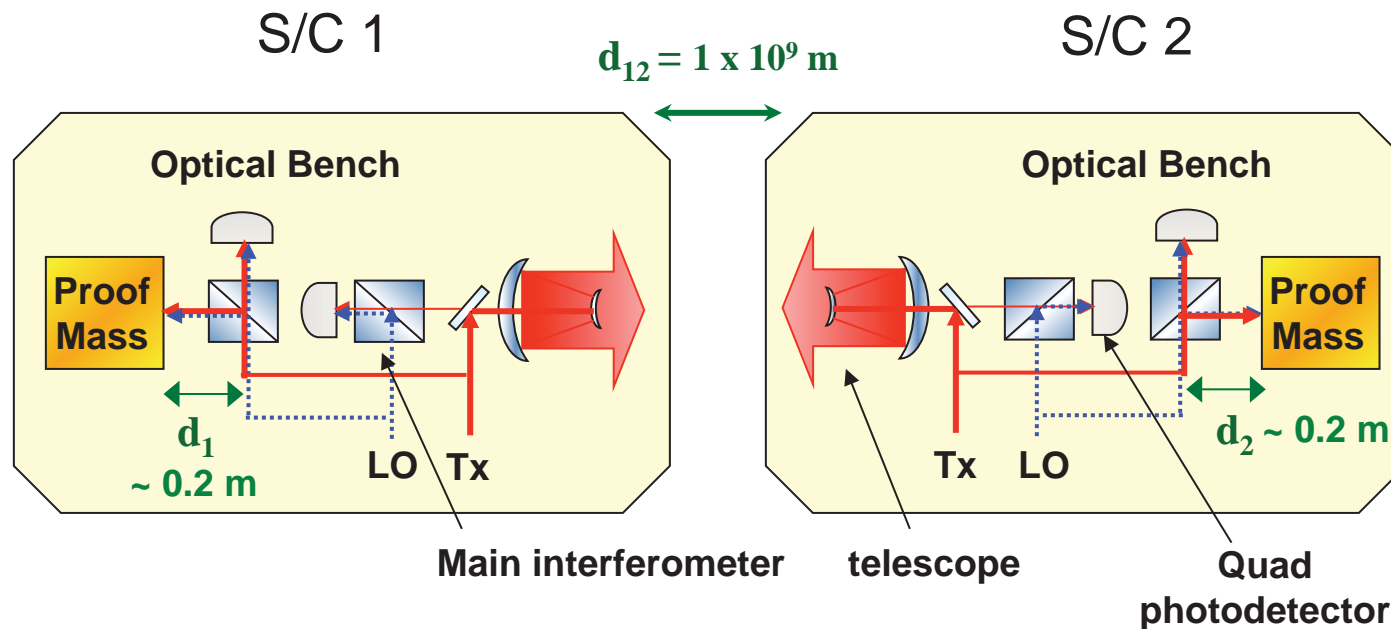
24 months science operations: orbits optimized for 48 months

Pre-Launch ♦ 18 month cruise ♦♦♦ Science Operations ♦

End of Mission

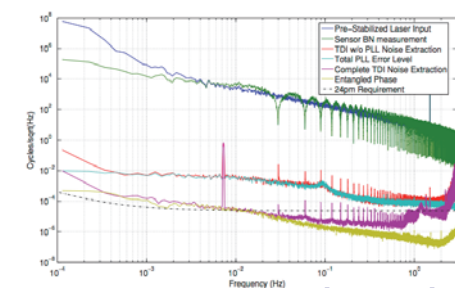
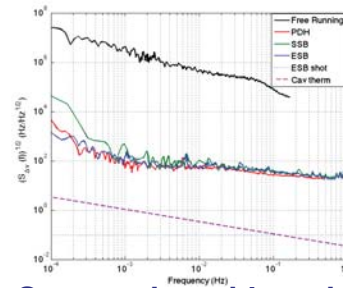
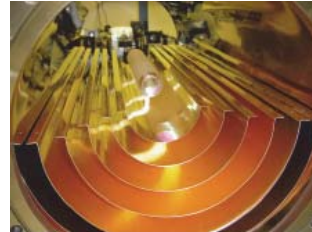
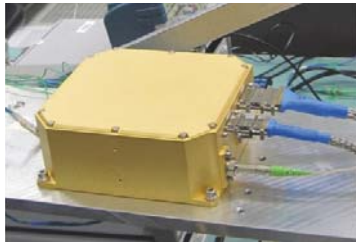
# Inter-Spacecraft Distance Measurement

- Test-mass to test-mass measured in 3 parts:
  - 2 × test-mass to spacecraft measurements (short-arm: LPF tests this)
  - 1 × spacecraft to spacecraft interferometer (long-arm)



# Interferometry Measurement System

LASER

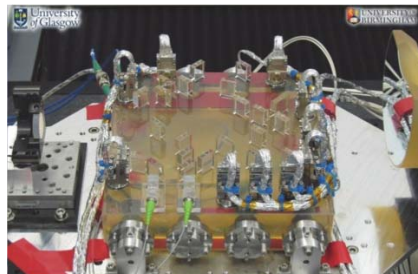


Seed laser with LPF heritage Cavity pre-stabilization

Same noise with tuning  
US Patent 7,970,025

TDI demonstrated with realistic delays using electronic signals

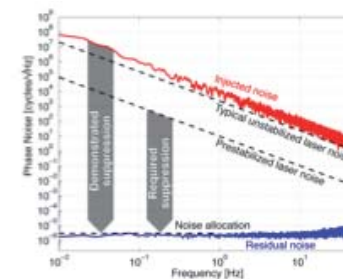
OPTICAL BENCH



Optical bench with LPF heritage



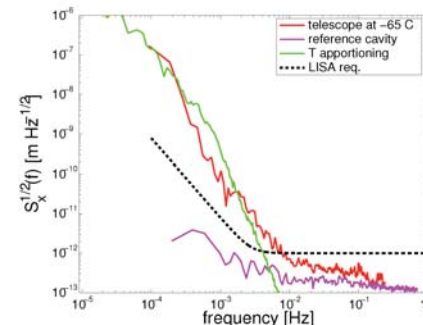
Low noise quad detector  
US Patent 8,598,673 B2



LISA Phasemeter development meets multiple requirements



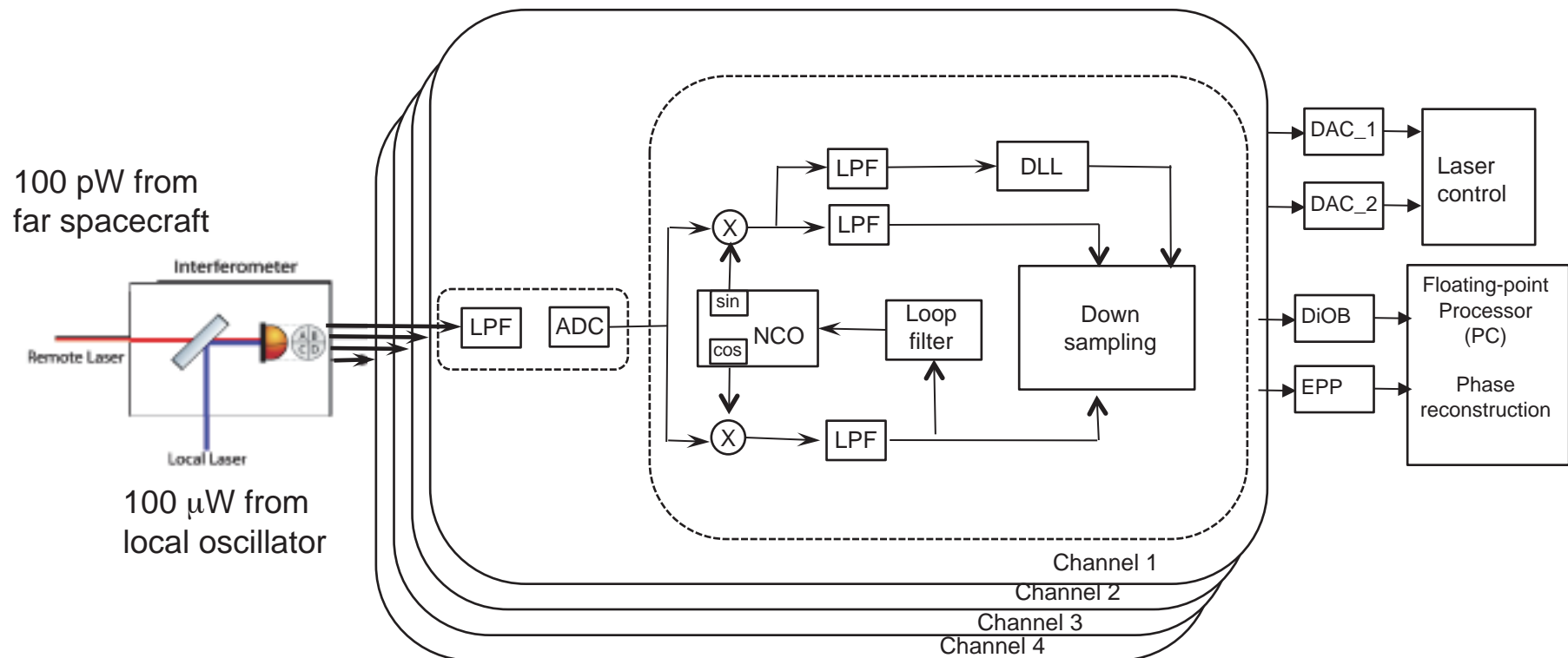
Pointing mechanisms tested



Prototype telescope spacer demonstrates dimensional stability and for studying scattered/stray light



# Front-end Phasemeter Architecture



- **Low noise quad photodiode\* serves two functions**
  - **Differential wavefront sensing of quadrant pairs determines S/C pointing**
  - **Sum is main science signal**

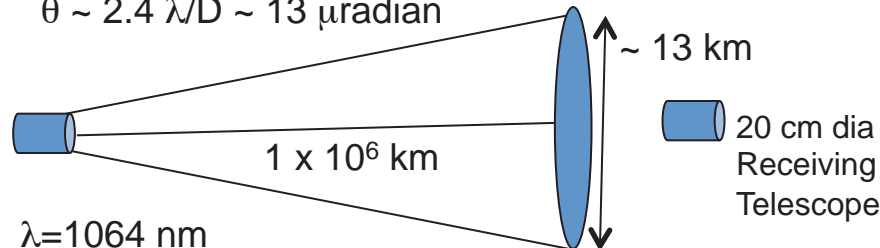
\*Joshi, A. et al. Proc. SPIE 8453, 84532G (25 Sep 2012);  
doi: [10.1117/12.918285](https://doi.org/10.1117/12.918285)



# Weak Light Phase Locking

SGO received power budget:

$$\theta \sim 2.4 \lambda/D \sim 13 \mu\text{radian}$$



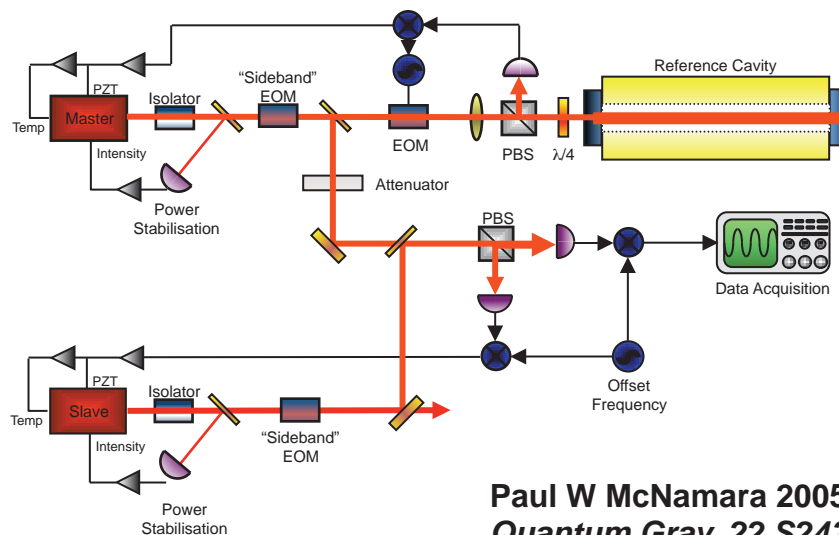
$$\lambda = 1064 \text{ nm}$$

$$D = 20 \text{ cm}$$

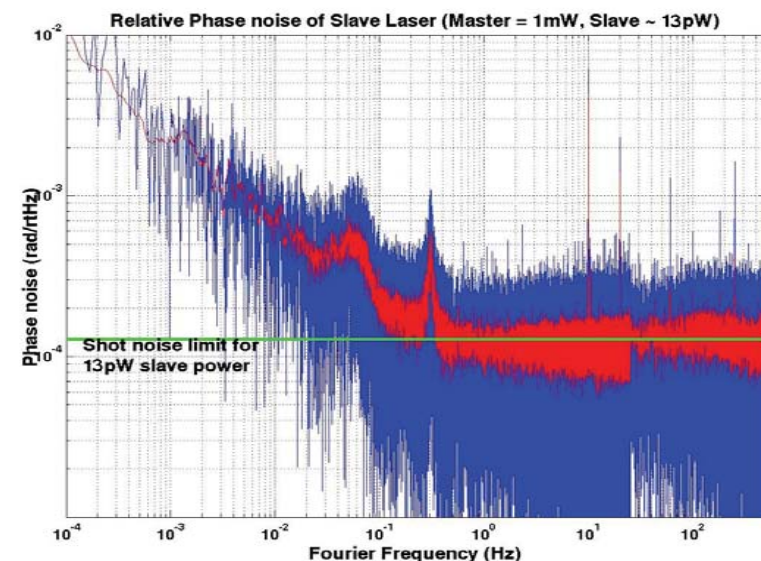
$$(20 \text{ cm}/13 \text{ km})^2 \sim 2.5 \times 10^{-10}$$

$$P_{TX} = 0.5 \text{ W} \rightarrow P_{RX} \sim 125 \text{ pW}$$

- Phase lock Successful at lower power than requirements
  - Master Oscillator = 1 mW vs 3-10 mW
  - Slave laser power = 13pW vs ~ 100 pW
  - Laser power step attenuated– not variable
- Shot noise limit for 13pW =  $1.3 \times 10^{-4} \text{ rad}/\sqrt{\text{Hz}}$



Paul W McNamara 2005 *Class. Quantum Grav.* 22 S243-S247

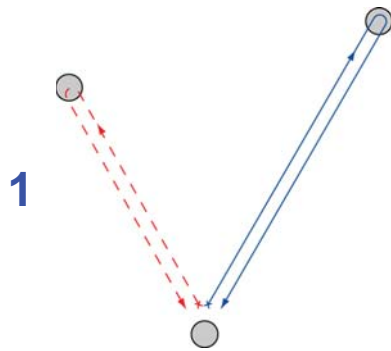




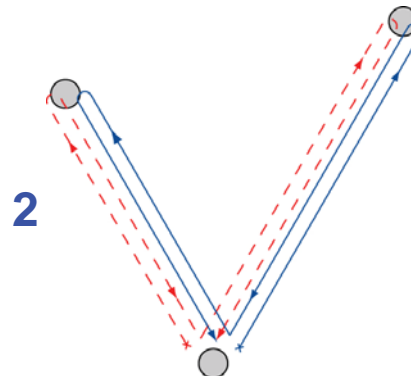
# Frequency Noise Suppression: Time Delay Interferometry (TDI)

- An interferometer arm length mismatch  $\Delta L$  will allow frequency noise to mimic a displacement noise,  $\delta x$ .
- A sensitivity requirement of  $\delta x < 10 \text{ pm}/\sqrt{\text{Hz}}$  implies that the interferometer arm lengths must be equal to better than 100 m
- LISA arm lengths may differ by as much as 1% or 10,000 km!

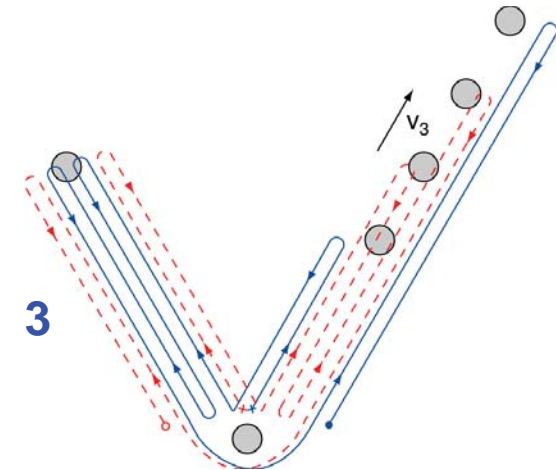
$$\delta x = \frac{\delta v}{v} \Delta L$$



- Unequal-arm Michelson interferometer
- Output corrupted by laser frequency noise



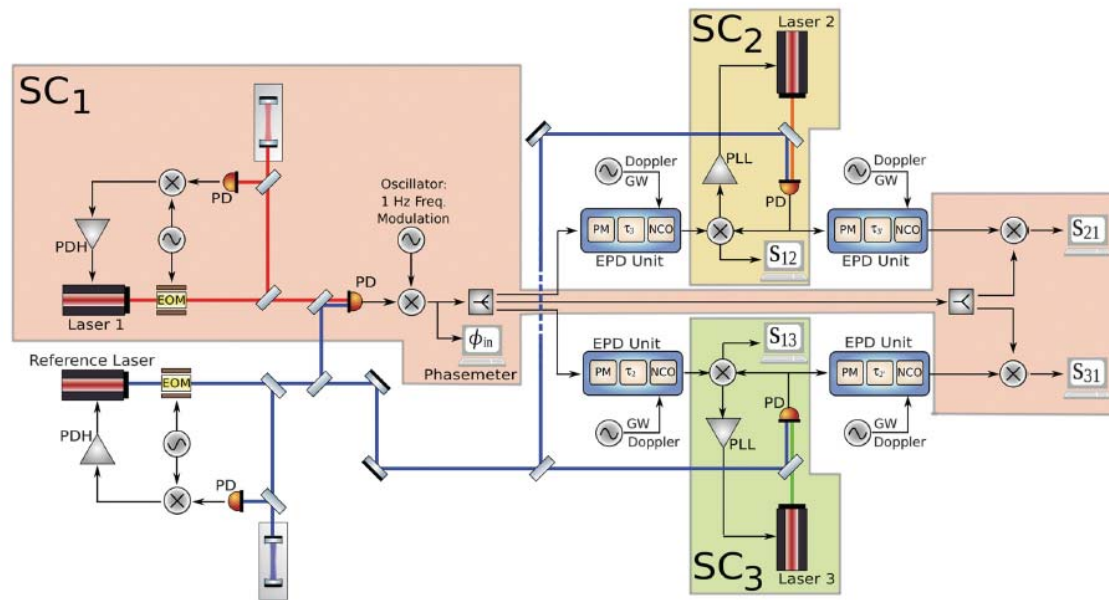
- Equal-arm (Sagnac) interferometer (TDI combination X)
- Output immune to laser frequency noise: synthesized equal arms



- Constant spacecraft velocity introduces an arm length mismatch to the synthesized interferometer.
- $\Delta L \sim 20 \text{ m/s} \times 6.7 \text{ s} \sim 130 \text{ m}$
- Output immune to laser frequency noise: synthesized equal arms

D.A. Shaddock, et al; PRD **68**, 061303 (2003).

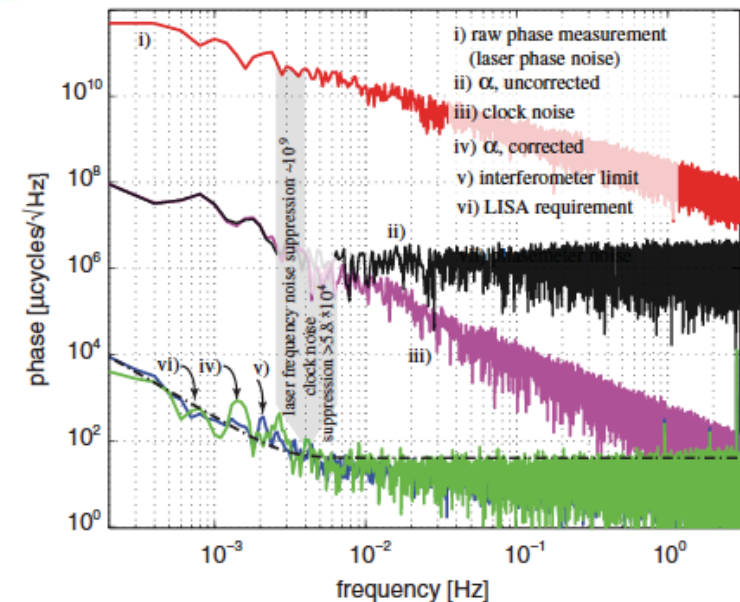
# TDI Experimental Demonstration



Mitryck, et al. PRD **86**, 122006 (2012) testbed with electronic delays

**Laser frequency noise can be reduced with margin**

- Laser frequency noise suppression of  $\sim 10^9$
- Clock noise suppression of  $\sim 6 \times 10^4$

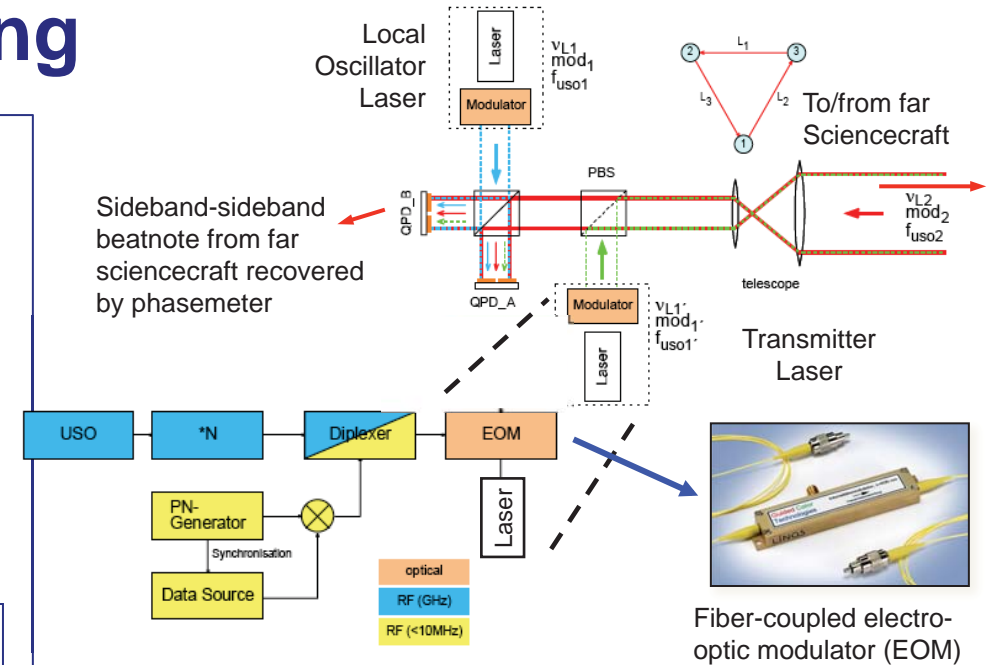
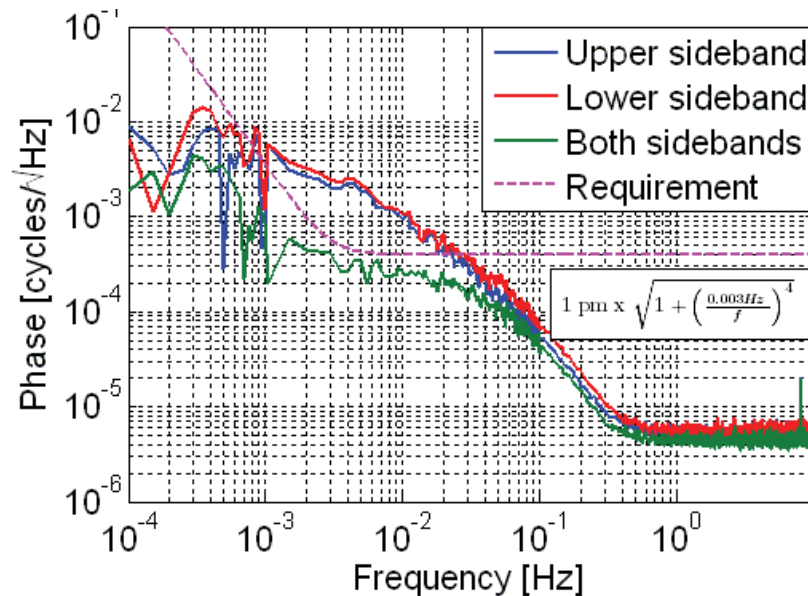


de Vine, et al. PRL **104**, 211103 (2010)  
static test bed

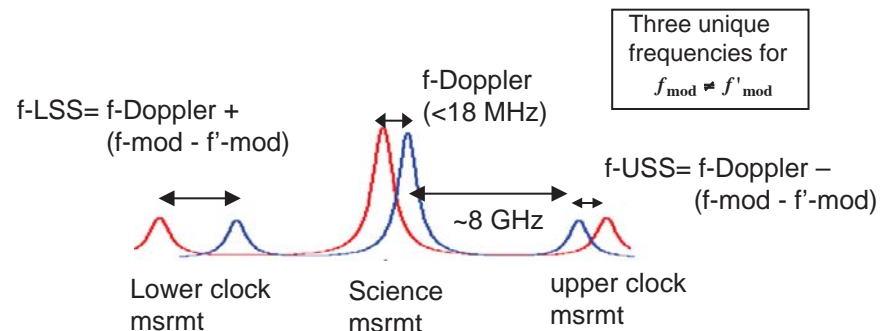
# Inter-Sciencecraft Signaling: Clock noise and ranging

- Requirement 1:
- Implementation: clock-coherent side tone
  - 8 GHz nominal sidetones (~2 MHz offsets in send vs receive)
  - 1% of power in sidebands
  - Sideband-sideband beat detection
- Requirement 2:
- Implementation: inter-spacecraft comm
  - 1% modulation on main science beam (carrier)
  - Manchester encoding (2 Mchips/s)
  - 13-bit Gold code yields 2 m range accuracy
  - ~100 bps required (400 kbps capable)

**Phase modulator supports clock noise rqmts**



Ultra-stable oscillator (USO) modulated onto main science beam



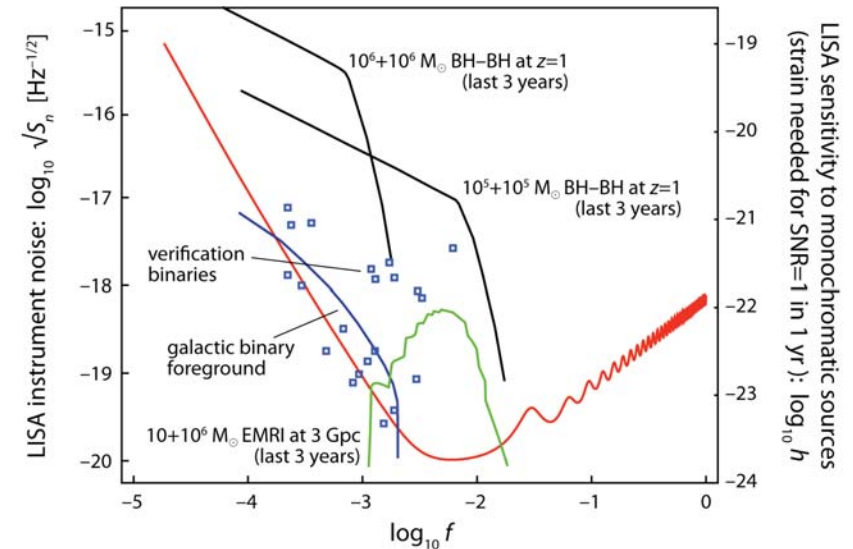
Using sideband-sideband beatnotes (instead of carrier-sideband) allows high modulation frequency and low photoreceiver BW

# Instrument Performance

- The instrument performance is determined by:
  - Displacement noise from the Interferometric Measurement System (IMS)
  - Acceleration noise from the Disturbance Reduction System (DRS)
  - Arm Length ( $1 \times 10^6$  km)
- The arm length also determines the instrument response function and is optimized for the science requirements.

Summary of DRS Subsystem allocations

	$\times 10^{-16} \frac{m}{s^2 \sqrt{Hz}} \sqrt{1 + \left(\frac{f}{8 \text{ mHz}}\right)^4} \sqrt{1 + \left(\frac{0.1 \text{ mHz}}{f}\right)^4}$	
Effect	Total per group	Per group
<b>Total Acceleration noise Budget</b>	<b>30.0</b>	
<b>Total of subsystem allocations</b>	<b>19.5</b>	
<b>Disturbance Groups</b>		
Electrostatics		12.0
Brownian		9.1
Spacecraft magnetic		7.0
Spacecraft coupling		6.0
Spacecraft cross coupling		4.5
Thermal		4.0
Interplanetary Magnetic		4.0
Misc small effects		4.0

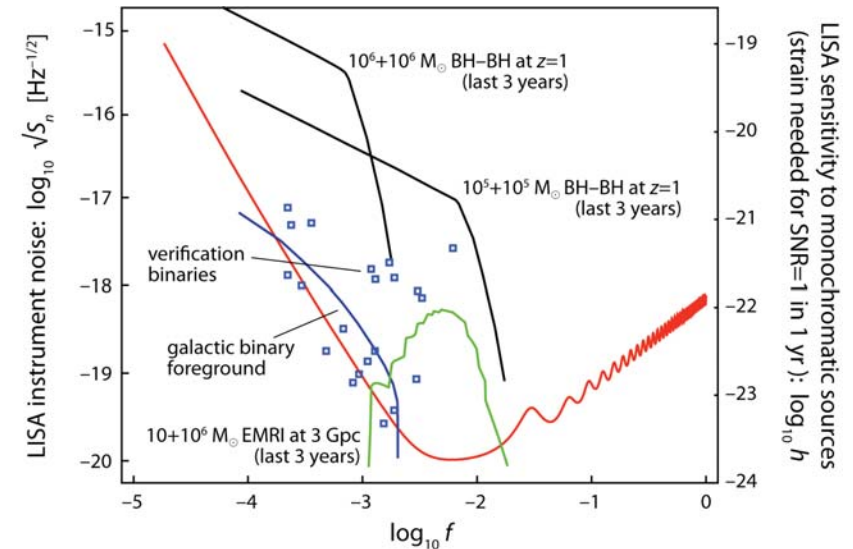


Summary of IMS subsystem noise allocations

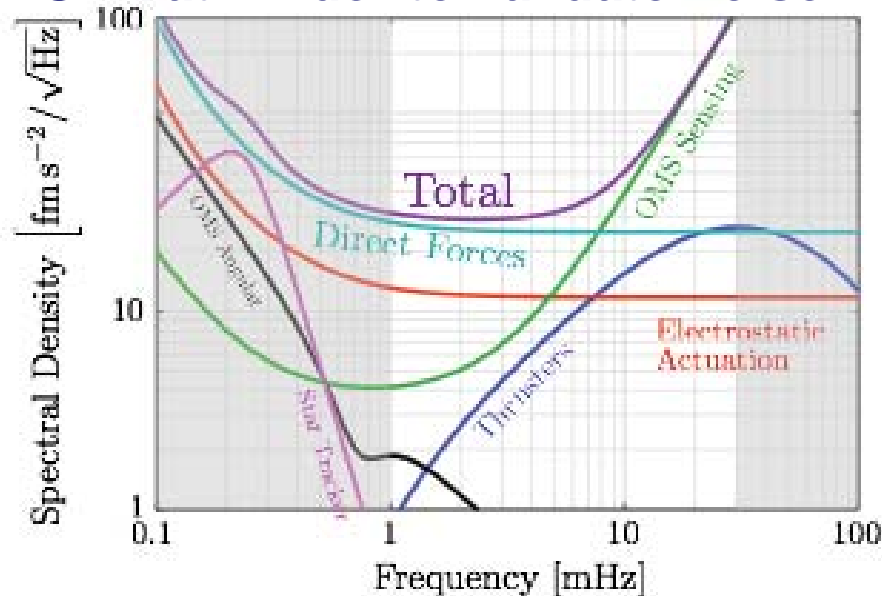
	$\times 10^{-12} \frac{m}{\sqrt{Hz}} \sqrt{1 + \left(\frac{2 \text{ mHz}}{f}\right)^4}$	
Effect	Total per group (pm/√Hz)	Sub - Allocation
<b>Total IMS Error/Noise Budget</b>	<b>12.0</b>	
<b>Total of subsystem allocations</b>	<b>11.7</b>	
<b>Subsystem Allocations</b>		
Shot noise	7.7	
Pathlength noise	7.0	
Pointing Errors		5.3
Telescope pathlength stability		1
Optical bench pathlength stability		4.5
<b>Measurement noise</b>	<b>5.4</b>	
Photoreceiver errors		3
Residual laser frequency noise		2
Residual clock frequency noise		3
Phasemeter noise		1
Intensity noise		1
Phase reconstruction		1
straylight		2

# Instrument Performance

- The instrument performance is determined by:
  - Displacement noise from the Interferometric Measurement System (IMS)
  - Acceleration noise from the Disturbance Reduction System (DRS)
  - Arm Length ( $1 \times 10^6$  km)
- The arm length also determines the instrument response function and is optimized for the science requirements.



## LISA Pathfinder to validate noise model



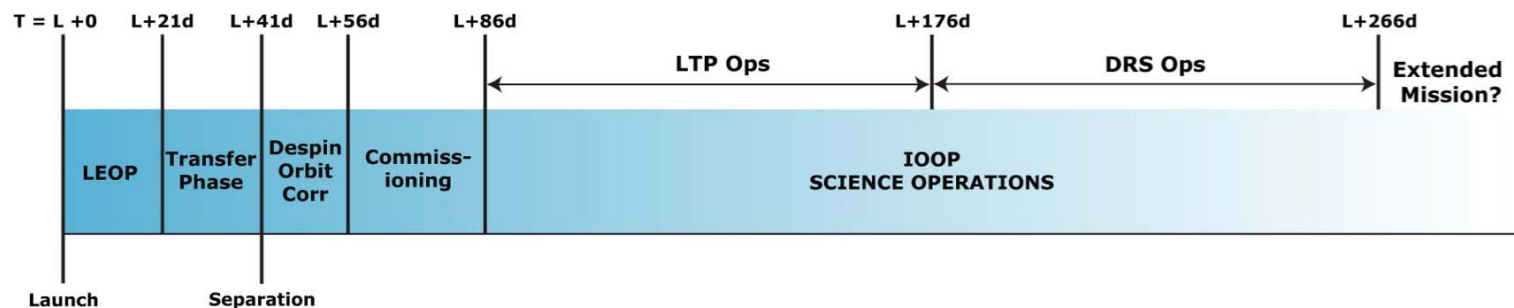
Summary of IMS subsystem noise allocations

	$\times 10^{-12} \frac{m}{\sqrt{Hz}} \sqrt{1 + \left(\frac{2 \text{ mHz}}{f}\right)^4}$	
Effect	Total per group (pm/ $\sqrt{Hz}$ )	Sub - Allocation
<b>Total IMS Error/Noise Budget</b>	<b>12.0</b>	
<b>Total of subsystem allocations</b>	<b>11.7</b>	
<b>Subsystem Allocations</b>		
Shot noise	7.7	
Pathlength noise	7.0	
Pointing Errors		5.3
Telescope pathlength stability		1
Optical bench pathlength stability		4.5
<b>Measurement noise</b>	<b>5.4</b>	
Photoreceiver errors		3
Residual laser frequency noise		2
Residual clock frequency noise		3
Phasemeter noise		1
Intensity noise		1
Phase reconstruction		1
straylight		2



# LPF Status

- Propulsion module complete
- Spacecraft bus near complete
  - cold-gas thruster system currently being integrated
- Major system tests complete
  - thermal
  - electro-magnetic
  - vibration/shock
- On-track for July 2015 launch
  - Lissajous orbit around L1
  - 90 days LTP Ops
  - 90 days DRS Ops





# Summary

---

- **Space-based gravitational-wave work continues**
  - Science receives top ratings in reviews
  - LPF is progressing for launch in July 2015
  - Issue is funding, not technology
- **Current opportunity is partnership with ESA on an L3 mission for 2034 launch**
  - 20+ year scientific collaboration on both sides of the Atlantic
- **Successful LISA Pathfinder technology demo required**
- **US technology development targeted at TRL-5 level for ~ 2020 for key technologies**

# BACKUP SLIDES

# Context and Status of SGO-Mid

---

- **No official project office at NASA**
  - Study team under Physics of the Cosmos Program office
- **No LISA International Science Team (LIST)**
  - University engagement is critical
  - Community engagement through PhysPAG
- **Technology development for L3 mission contribution**
  - laser                                      -- photoreceiver
  - telescope                                      -- micro-newton thruster
  - phasemeter
- **Participation on LPF science team**
  - ST-7 experiments                      -- mission data analysis operations
- **Developing a reference mission and science case**

# SGO-High vs Mid (vs LISA baseline)

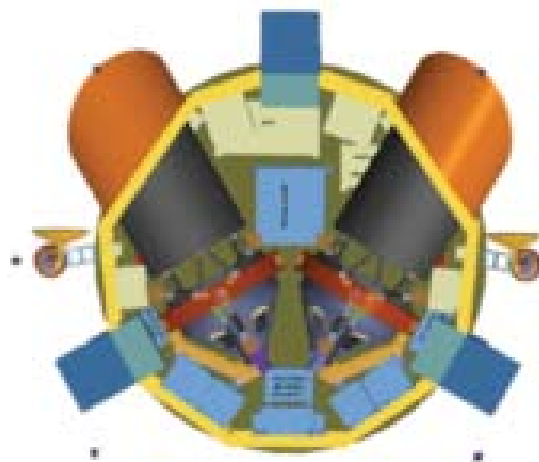
- SGO High differs from LISA by:

- Preserves all LISA performance parameters
- Single agency cost model (not joint mission)
- Lower cost launch vehicle (shared launch on a Falcon Heavy)
- Demonstrated improvements in photoreceiver performance
- More economical trajectories to the operational orbits

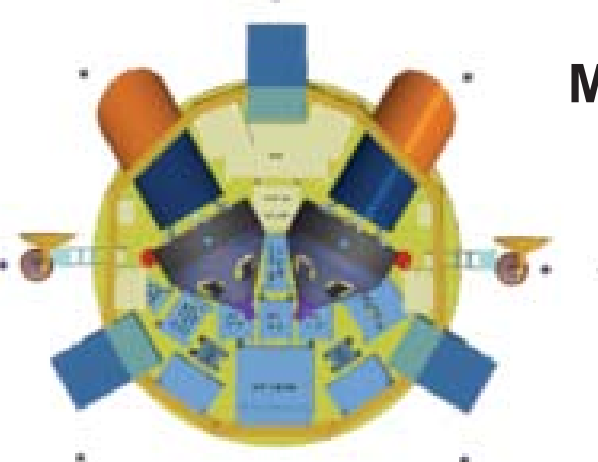
- SGO Mid differs from LISA by:

- Detector arm length reduced from 5 Gm to 1 Gm
- Science operations reduced from 5 to 2 years.
- Nominal starting distance from Earth is reduced by about a factor of 2.5 to a 9-degree trailing orbit.
- Telescope diameter is reduced from 40 to 25 cm, and the laser power out of the telescope is reduced from 1.2 to 0.7 W (end of life).
- In-field guiding is used instead of articulating the entire optical assembly

High



Mid



# LISA vs SGO-high vs SGO-mid

Parameter	LISA Concept	SGO High	SGO Mid
Arm length (meters)	$5 \times 10^9$	$5 \times 10^9$	$1 \times 10^9$
Constellation	Triangle	Triangle	Triangle
Orbit	22° heliocentric, earth-trailing	22° heliocentric, earth-trailing	Heliocentric, earth-trailing, drifting-away 9°- 21°
Trajectory	Direct injection to escape, 14 months	Direct injection to escape, 14 months	Direct injection to escape, 18 months
Interferometer configuration	3 arms, 6 links	3 arms, 6 links	3 arms, 6 links
Launch vehicle	Medium EELV (e.g., Atlas V 431)	Medium EELV (e.g., Falcon Heavy shared launch)	Medium EELV (e.g., Falcon 9 Block 3)
Baseline/Extended Mission Duration (years)	5/3.5	5/3.5	2/2
Telescope Diameter (cm)	40	40	25
Laser power out of telescope end of life (W)	1.2	1.2	0.7
Measurement system modifications	Baseline/Reference	Baseline/Reference (Same as LISA Concept)	In-field guiding, UV-LEDs, no pointing
Motivation:	Science performance, two agencies	LISA performance with all known economies	Lowest cost 6 links
Approximate Cost (FY12 \$B)	1.82	1.66	1.40

# Orbits/trajectory

- **2 year drift-away**
  - ~ 6 deg/year drift rate starting at 9 degrees
  - 2 year end of mission similar to nominal SGO-high orbital station (but orbit optimized for 4 years)
  - EOL communications requirements similar to SGO-high
- **Stable constellation geometry simplifies measurement**
  - $\Delta L/L \sim 0.010$ , relative to  $10^6$  km
  - $\Delta \alpha \sim \pm 0.6^\circ$  relative to  $60^\circ$
  - $\Delta v \sim \pm 1.6$  m/s
  - Point ahead  $\sim \pm 0.55$  urad out of plane
  - Point ahead  $\sim \pm 0.004$  urad in plane, relative to  $\sim -0.3$  urad
- **18 month trajectory from escape**
  - For shared launch, second stage has 2 restarts
  - Drop off shared package at GTO, then go to escape
  - Optimized  $\Delta V \sim 130$  m/s (each),  $\sim 200$  m/s for extended launch window and margin



# Operations / Science Data

---

- **Simple Operations**

- No instrument pointing or scheduling of observation time
- LISA observes “all the sky, all the time”
  - Scheduled interruptions approximately every 2 weeks for HGA re-pointing and to switch laser offset frequencies

- **Routine Communications Strategy**

- Ka-Band downlink every 2 days with one spacecraft (6 days for the constellation)
- Up to 8-hr contacts with DSN 34m at 90 kbps (allows downlink of 6 days telemetry generated at 5 kbps)
- Special merger events may require more frequent contact and continuous operation for up to ~ 4 days to preempt schedule interruptions and com

- **Science Data**

- 5 kbps = 1 kbps science data + 4 kbps science housekeeping and engineering data, 15 kbps total for the constellation
- **No on-board science processing**
- Mission Ops Team forwards downlinked data to Science Data Centers

# Countering Solar Radiation Pressure

## Drag-free control

Thrusters

Satellite

Satellite

Position

sensor

Test mass

X

Control loop

